## Discriminants and $x$-intercepts

NAME:
There are three possibilities for the number of $x$-intercepts of a quadratic function: two, one, or zero. Fill in the following table to develop examples for these three possibilities. Choose small enough values for $\mathbf{a}, \mathbf{b}$, and $\mathbf{c}$ so that you can do the operations in your head.

| Function | Discriminant <br> $\mathbf{b}^{2}-\mathbf{4 a c}$ | Graph | Number of <br> $\boldsymbol{x}$-intercepts |
| :--- | :--- | :--- | :--- |
|  | $\mathbf{b}^{2}-\mathbf{4 a c}=\mathbf{0}$ |  |  |
|  | $\mathbf{b}^{2}-\mathbf{4 a c}<\mathbf{0}$ |  |  |
|  |  |  |  |
|  | $\mathbf{b}^{2}-\mathbf{4 a c}>\mathbf{0}$ |  |  |

1. To form a function that will guarantee $\mathbf{b}^{2}-\mathbf{4 a c}=\mathbf{0}$, do the following.

Select $\mathbf{b}$ to be an even number. Then divide $\mathbf{b}^{2}$ by 4 . Choose $\mathbf{a}$ and $\mathbf{c}$ so that their product is equal to the quotient $\frac{b^{2}}{4}$.
2. To form a function that will guarantee $\mathbf{b}^{2}-\mathbf{4 a c}<\mathbf{0}$, do the following.

Select $\mathbf{b}$ to be an even number. Then divide $\mathbf{b}^{2}$ by 4 . Choose $\mathbf{a}$ and $\mathbf{c}$ so that their product is greater than the quotient $\frac{b^{2}}{4}$.
3. To form a function that will guarantee $\mathbf{b}^{2}-\mathbf{4 a c}>\mathbf{0}$, do the following.

Select $\mathbf{b}$ to be an even number. Then divide $\mathbf{b}^{2}$ by 4 . Choose $\mathbf{a}$ and $\mathbf{c}$ so that their product is less than the quotient $\frac{b^{2}}{4}$.
4. For each function, calculate $\mathbf{b}^{\mathbf{2}} \mathbf{- 4 a c}$ in the second column, graph the function in the third column (standard window should be fine), and denote the number of $x$ intercepts in the fourth column.

