We will see how differences in successive $y$-values for a function can help you find its formula.

1. Complete the table for the function, finding the difference between each two $y$-values.

2. If we were not given the formula $y=4 x+6$ for this function, how could we guess it from the table? In other words, for the generic formula $y=f \cdot x+e$, how would you guess $f$ and $e$ ?
3. Try out your method to find the formula for the following function shown in the table below.

| $\boldsymbol{x}$ | $\boldsymbol{y}=\mathbf{f} \cdot \boldsymbol{x}+\mathbf{e}$ | Difference between $\boldsymbol{y}$-values |
| :---: | :---: | :---: |
| 0 | 14 |  |
| 1 | 16 |  |
| 2 | 20 |  |
| 3 | 24 |  |
| 5 |  |  |
| 2 |  |  |


4. One reason you might want to determine a function's formula is to find $y$-values for other $x$-values that are not near the table. Use the formula you found in the last question to find the $y$-value when $x$ is 25 .
5. Let's investigate another type of function. Complete the table of finite differences below, but this time, we do it in general using the quadratic function $y=g x^{2}+f x+e$. We will also find the differences of those differences, shown in the fourth column.


6a. Do you see the pattern? How would you use the table to find the value of $e$ ? Circle the entry in the table where $e$ appears alone.

6 b . How do we find the value of $g$ ? Circle the entries in the table that would be the easiest to use.

6c. If we know $g$, could you figure out what $f$ has to be? Circle the entry in the table that would be the easiest to use.
7. Let's see this in action with a specific function.

| $x$ | $y=2 x^{2}+3 x+5$ | Difference between $y$-values | Difference between entries in previous column (differences) |
| :---: | :---: | :---: | :---: |
| 0 | 5 |  |  |
| 1 | 10 |  |  |
| 2 | 19 |  |  |
| 3 | 32 |  |  |
| 4 | 49 |  |  |
| 5 | 70 |  |  |

8. Recall the formula for the relationship in the previous question is $y=2 x^{2}+3 x+5$. Here, we are using the numbers 2,3 , and 5 for the variables $g$, $f$, and $e$, respectively. Let's see how the values of 2,3 , and 5 show up in the table.

To find $e$ (or 5): The $y$-value for the $x$-value of 0 (which is the first entry in the $y$ column) happens to be 5. Circle this table entry. [We saw this in general for number 6 a above.]

To find $g$ (or 2): Notice that all of the entries in the fourth column (differences of the differences) are all "twice 2". Circle these table entries. [We saw this in general for number 6 b above.]

To find $f$ (or 3): Likewise from numbers 5 and 6 , do you remember where " $\mathrm{f}+\mathrm{g}$ " was located in the table? Find that location in this table (circle it) and show how 3 is contained within it.
9. Use this process to find the formula for the function below.

| $x$ | $y=g x^{2}+f x+e$ | Difference between $y$-values | Difference between entries in previous column (differences) |
| :---: | :---: | :---: | :---: |
| 0 | 9 |  |  |
| 1 | 16 |  |  |
| 2 | 29 |  |  |
| 3 | 48 |  |  |
| 4 | 73 |  |  |
| 5 | 104 |  |  |

Be sure to write the formula of the function. Remember that is the whole point of analyzing the table.

10 . For the function in the previous question, what is the $y$-value when the $x$-value is 14 ?

