

There are many applications where we need to multiply fractions.

How do we find $\frac{1}{2}$ of $\frac{1}{3}$? First, we will look at a picture.

Now, we want $\frac{1}{2}$ of this $\frac{1}{3}$ that is pictured. Cut the shaded piece equally in half and shade one of the pieces. What fraction of the original area do we now have?



Calculation-wise: If we multiply the fractions' tops and bottoms separately, we will get the $\frac{1}{6}$ we know to be the answer. Try it out here.

Mnemonic device: To find $\frac{1}{2}$ of $\frac{1}{3}$, we think of the "of" as "multiply".

expl 1: Multiply and write in lowest terms.

$$\frac{4}{7} \times \frac{5}{6}$$

We'll always want the final answer in lowest terms.

Two Different Methods (When Top and Bottom Have Common Factors):

1. Multiply the fractions' tops and bottoms separately, *then* reduce to lowest terms.

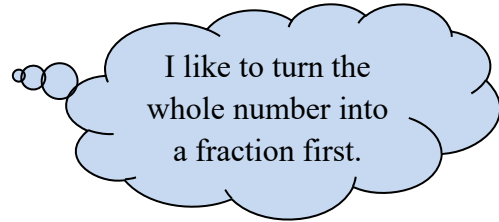
Try the method you did *not* do above.

2. Reduce any common factors from top and bottom first, *then* multiply.

Which do you prefer?

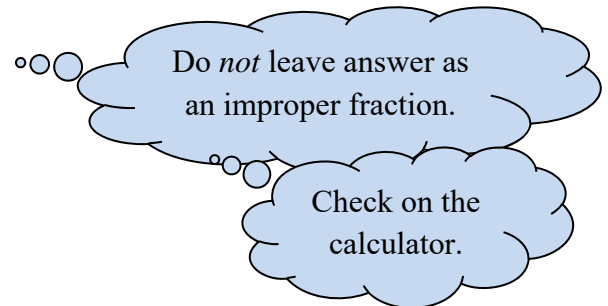
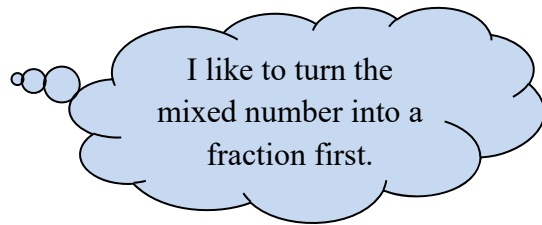
expl 2: Multiply and write in lowest terms.

$$10 \times \frac{3}{4}$$



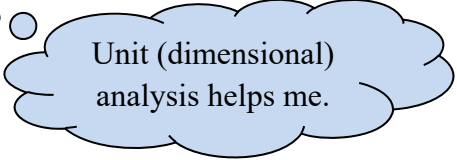
expl 3: Multiply and write in lowest terms.

$$11 \frac{6}{7} \times \frac{7}{8}$$



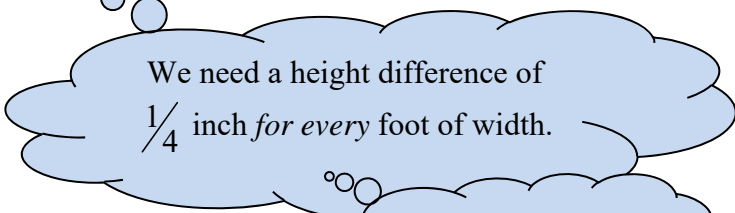
expl 4: How far will a nut advance if it is given 18 turns on a $\frac{1}{4}$ -in. 20-NF (National Fine thread) bolt? (The designation 20-NF means the nut will advance $\frac{1}{20}$ in. for each complete turn.)

expl 5: How many pounds of grease are contained in a barrel if the barrel holds $46 \frac{1}{2}$ gallons?
Each gallon of grease weighs $7 \frac{2}{3}$ lb. Give your answer as a whole number, proper fraction, or mixed number.

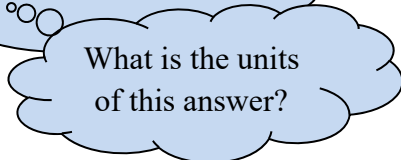


Unit (dimensional) analysis helps me.

expl 6: A patio $15 \frac{1}{2}$ feet wide is being constructed next to a house. To drain water away from the house, a slope of $\frac{1}{4}$ inch per foot is needed. What total difference in height is required from one edge of the patio to the other?



We need a height difference of $\frac{1}{4}$ inch *for every* foot of width.



What is the units of this answer?

expl 7: What is the height of 12 courses of $2 \frac{1}{4}$ -in. bricks with $\frac{3}{8}$ -in. mortar joints? (Twelve courses mean there will be 12 rows of brick and 11 mortar joints.)