College algebra Library of Functions and Piecewise Functions Section 3.4

Library of Functions:

Draw from memory or use your calculator (on the Standard window) to graph the following functions. You should acquaint yourself with their basic shapes.

Identity function	Square function	Square root function
y = x	$y = x^2$	$y = \sqrt{x}$
Cube function $y = x^3$	Cube root function $y = \sqrt[3]{x}$	Constant function y = b, b is a real number b . Make up b .
Absolute value function y = x	Reciprocal function $y = \frac{1}{x}$	Greatest integer function y = int(x) = greatest integer less than or equal to x Use tick marks.

Where are these functions increasing, decreasing, constant? Where are their (x and y) intercepts? Later, we will study how to transform these graphs by shifting, reflecting, stretching, and shrinking (also called compressing or squashing) the graphs.

Properties of Base Functions:

For each of the functions above, we will investigate several questions. Consult the information below. (I abbreviated increasing/decreasing/constant as inc/dec/cnst.)

Identity function	Square function	Square root function
y = x	$y = x^2$	$y = \sqrt{x}$
domain: $(-\infty,\infty)$	domain: $(-\infty,\infty)$	domain: $[0,\infty)$
range: $(-\infty,\infty)$	range: $[0,\infty)$	range: $[0,\infty)$
x-intercept(s): $x = 0$	x-intercept(s): $x = 0$	x-intercept(s): $x = 0$
y-intercept: $y = 0$	y-intercept: $y = 0$	y-intercept: $y = 0$
even or odd?: odd	even or odd?: even	even or odd?: neither
inc/dec/cnst?: inc: $(-\infty,\infty)$	inc/dec/cnst?: dec: $(-\infty, 0]$	inc/dec/cnst?: inc: $[0,\infty)$
	inc: $[0,\infty)$	
mins/maxes: none		mins/maxes: abs. min. of
	mins/maxes: abs. min. of y = 0 at $x = 0$	y = 0 at x = 0
	y = 0 at $x = 0$	y = 0 at $x = 0$
Cube function	Cube root function	Constant function
$y = x^3$	$y = \sqrt[3]{x}$	y = b, b is a real number
domain: $(-\infty,\infty)$	domain: $(-\infty,\infty)$	domain: $(-\infty,\infty)$
range: $(-\infty, \infty)$	range: $(-\infty, \infty)$	range: { <i>b</i> }
x-intercept(s): $x = 0$	x-intercept(s): $x = 0$	x-intercept(s): none unless $b = 0$
y-intercept: $y = 0$	y-intercept: $y = 0$	y-intercept: $y = b$
even or odd?: odd	even or odd?: odd	even or odd?: even
inc/dec/cnst?: inc: $(-\infty,\infty)$	inc/dec/cnst?: inc: $(-\infty, \infty)$	inc/dec/cnst?: cnst: $(-\infty,\infty)$
mins/maxes: none	mins/maxes: none	mins/maxes: abs. min. and abs. max. of $y = b$ for all x
Absolute value function	Reciprocal function	Greatest integer function
y = x	$y = \frac{1}{2}$	y = int(x) = greatest integer less
domain: $(-\infty,\infty)$	$\int \frac{y}{x}$	than or equal to x
range: $[0,\infty)$	domain: $(-\infty, 0) \cup (0, \infty)$	domain: $(-\infty,\infty)$
x-intercept(s): $x = 0$	range: $(-\infty, 0) \cup (0, \infty)$	range: $\{y \mid y \text{ is an integer}\}$
y-intercept: $y = 0$	<i>x</i> -intercept(s): none	x-intercept(s): $0 \le x < 1$ y-intercept: $y = 0$
even or odd?: even	y-intercept: none	y-intercept: $y = 0$ even or odd?: neither
inc/dec/cnst?: dec: $(-\infty, 0]$	even or odd?: odd	inc/dec/cnst?: cnst: every
inc: [0,∞)	inc/dec/cnst?: dec: $(-\infty,0) \cup (0,\infty)$	interval of the form $[k, k+1)$ for k an integer
mins/maxes: abs. min. of y = 0 at $x = 0$	mins/maxes: none	mins/maxes: none

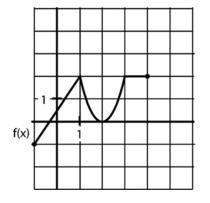
expl 1: For the function f(x) = int(3x), find the following. a.) f(2.3) b.) f(2)

expl 2: For the function $f(x) = \frac{1}{x}$, find the following. a.) f(5) b.) f(0)

expl 3: For the function f(x) = 5, find the following. a.) f(2.3) b.) f(2)

Piecewise Functions:

The following is an example of a piecewise function. The idea here is that the function's *rule changes depending on which piece of the domain you're in.*

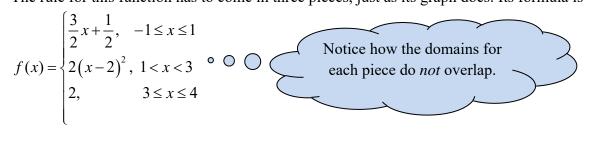


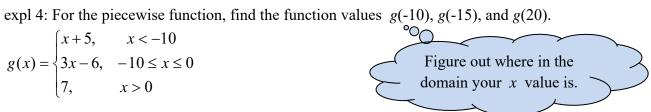
First, verify that this is, indeed, a function.

What is the domain of this function?

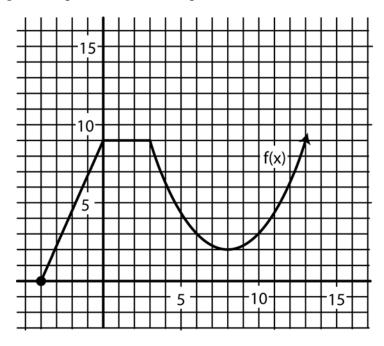
Break up this graph into its three pieces and determine the *x*-values (domains) for those pieces.

The rule for this function has to come in three pieces, just as its graph does. Its formula is





expl 5a: Determine the domain and range of the piecewise function pictured here.



expl 5b: Find f(10).

expl 6: For the function below to the right, complete the following.

 $g(x) = \begin{cases} 3x+3, & x<0\\ x+5, & x \ge 0 \end{cases}$

- a.) Find the domain.
- b.) Locate the intercepts.
- c.) Graph the function.
- d.) Find the range based on the graph.

You graph this piecewise function by graphing your first rule for x < 0 and your second rule for $x \ge 0$.

You can pick any points to graph but you should include endpoints and intercepts when you can.



Worksheet: Piecewise Functions:

We will practice using and graphing piecewise functions.