

Expected Value of Lottery Ticket

NAME:

The Illinois Lotto consists of six numbers chosen from 1 to 54. The table below has the prizes and the associated probabilities for Lotto (1999 Illinois Lottery pamphlet).

<b>How to Win Lotto</b>	<b>Probability</b>	<b>Prize</b>
<b>Grand Prize:</b> Match all six numbers in any order	.00000007744	\$2 million
<b>Second Prize:</b> Match five of the six numbers in any order	.00002230	\$2500
<b>Third Prize:</b> Match four of the six numbers in any order	.00131	\$75
<b>Overall Probability</b> of winning a prize	.00133	***

Consider that it costs \$1 to buy a ticket. Complete the table below by finding the probability of a losing ticket and the actual prize winnings for each of the four possibilities.

<b>How to Win Lotto</b>	<b>Probability</b>	<b>Actual Prize Winnings</b>
<b>Grand Prize:</b> Match all six numbers in any order	.00000007744	
<b>Second Prize:</b> Match five of the six numbers in any order	.00002230	
<b>Third Prize:</b> Match four of the six numbers in any order	.00131	
<b>Losing Ticket:</b> did not get any of the above winning combinations		

1. Now let  $X$  be the actual prize winnings from the ticket. Calculate the expected value of  $X$ . This is the expected value of a lottery ticket from the consumer's perspective. Show work.

2. Does it surprise you that the expected value is negative? Why should it be?

3. What does it mean for the consumer, on average, if the expected value of a lottery ticket is negative?